2914/102 2915/102 MATHEMATICS AND APPLIED SCIENCE Oct./Nov. 2019 Time: 3 hours



THE KENYA NATIONAL EXAMINATIONS COUNCIL

DIPLOMA IN APPLIED BIOLOGY DIPLOMA IN ANALYTICAL CHEMISTRY MODULE I

MATHEMATICS AND APPLIED SCIENCE

3 hours

INSTRUCTIONS TO CANDIDATES

This paper consists of 4 printed pages.

Candidates should check the question paper to ascertain that all the pages are printed as indicated and that no questions are missing.

SECTION A (60 marks)

Answer ALL the questions in this section.

1. Find the value of x in the equation;

$$\log_x 20 + \log_x 5 = 2. \tag{4 marks}$$

- 2. A swimmer can swim in still waters at 12 metres/ minute. In Tana River, the swimmer swam upstream for 100 m and back to the starting point and he took a total of 20 minutes. Determine the speed of the water downstream. (4 marks)
- 3. Find the value of x in $\frac{2^x \times 3^x}{12^x} = \frac{1}{8}$. (4 marks)
- 4. An arithmetic series has the terms 3, 7, 11, 15 99. Find the sum of all the terms.

$$S_n = 25 + (0-1)^2$$
 (4 marks)

- 5. Define the following terms as used in statistics:
 - (a) mean; (1 mark)
 - (b) median; (1 mark)
 - (c) assumed mean; (1 mark)
 - (d) degrees of freedom. (1 mark)
- 6. Solve the following simultaneous equations:
 - (a) 5x + 184y = 180
 - (b) $\frac{7x}{8} \frac{2}{1} + \frac{3y}{2} + 6 = \frac{6x}{7} \frac{3}{1} + \frac{2y}{5}$ (4 marks)
- 7. Evaluate the following matrix.

$$\begin{pmatrix} 3 & 1 & 1 \\ 4 & 7 & 8 \\ 11 & 9 & 0 \end{pmatrix} \quad \begin{pmatrix} 8 & 4 & 5 \\ 6 & 1 & 2 \\ 0 & 3 & 9 \end{pmatrix}.$$

(4 marks)

8. Differentiate the following function from the first principles;

$$f(x) = x^3 + 2x^2 + 7x + 5$$
 (4 marks)

9. Determine dimensionally, whether the equation $v^2 = u^2 + 2as$ is valid. The symbols v, u, a and s represent final velocity, initial velocity, acceleration and displacement respectively.

(4 marks)

10. (a) State the law of conservation of momentum.

(1 mark)

- (b) A 3.0 kg object is moving at a speed of 5.0 m/s. Determine:
 - (i) the force needed to stop the object in a time of 6.5×10^{-4} seconds; (2 marks)
 - (ii) impulse. (1 mark)
- 11. Figure 1 shows a system at equilibrium. The cylinder on the left side has a mass of 800 kg and cross-section area of 100 cm². The piston on the right side has a cross-section area of 32 cm² and negligible weight. The apparatus in filled with liquid of density 0.75 g/cm³.

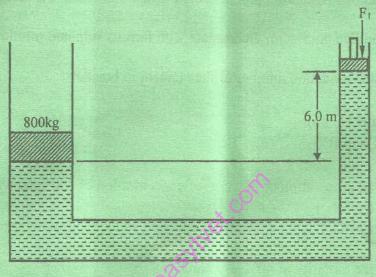


Fig. 1

Determine the force F₁.

(4 marks)

- 2. A thermo flask contains 300 g of liquid coffee at 85 °C. 25 g of milk at 10°C is added.

 Determine the temperature of liquid at equilibrium assuming no heat is lost (Specific heat capacity of coffee and milk are equal).

 (4 marks)
- 13. (a) State Newton's law of cooling.

(1 mark)

- (b) A spherical body of 3.0 cm diameter is maintained at 500 °C. Assuming that it radiates as if it were a black body, determine the rate of radiation. (stefan constant = $5.67 \times 10^{-8} Wm^{-2}K^{-4}$) (3 marks)
- 14. A wire that has a resistance of 10Ω is deformed such that the new length is three times the original length. Determine the new resistance. (4 marks)

15. (a) State Lenz's law.

(1 mark)

(b) Determine the critical angle for light passing from glass to water if the refractive index of glass and water are 1.54 and 1.33 respectively. (3 marks)

SECTION B (40 marks)

Answer ALL the questions in this section.

16. (a) Write balanced ionic equations for the reaction between:

- (i) acidified potassium permanganate with oxalic acid solutions. (2 marks)
- (ii) acidified potassium dichromate with ferrous sulphate solutions. (2 marks)

(b) Calculate the oxidation number of the element in brackets:

- (i) $Na_2S_3O_6$ (S) (2 marks)
- (ii) KClO₄ (Cl). (1 mark)

(c) Describe the preparation of 200 cm³ of concentration of 100 ppm with respect to copper using AR Cu(NO₃)₂.

(Cu = 63.5, N = 14, O = 16) $\frac{1}{8}$ (9 marks)

(d) Calculate the molarity of 40% w/v NaOH. (Na = 23, O = 16, H = 1)

(4 marks)

17. (a) Explain the importance of transpiration in plants. (6 marks)

- (b) Draw a transverse section of a typical dicotyledon leaf as seen under the compound light microscope. (10 marks)
- (c) Illustrate the genetic test-cross of the F1 of a dominant tall plant and a recessive dwarf plant. (4 marks)

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